

# A Global Predication Compilation Framework

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# Outline

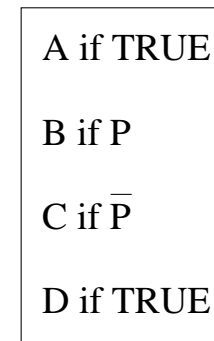
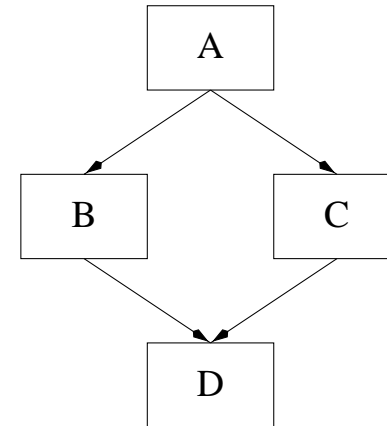
- Predication Background
- Predication Frameworks
- Predicate Optimization
  - Fully Resolved Predicates
  - Code Specialization
  - Control Logic Optimization
- Ultrablock Predication Framework
- Predicate Analysis
- Predicate Dataflow

## Predication Overview

- Conditional execution of an instruction based on a Boolean source operand
- Execution model
  - $r1 = r1 + 1 \langle p1 \rangle$
  - If p1 is TRUE, r1 is incremented.
  - If p1 is FALSE, r1 is unchanged.
- Provides the compiler with an alternative to guarding instructions with conditional branches.
- Levels of predication support
  - Full Predication Support
    - \* Predicate defining instructions
    - \* Full set of predicated instructions
    - \* Separate register file
  - Partial Predication Support - Existing ISA is enhanced with instructions such as CMOV or SELECT.
  - Dynamic Predication Support - ISA is unchanged.

# Predication

- Architectures supporting predication:
  - Illiac IV - vector masks
  - Cydrome's Cydra 5 - full predication
  - HPL's PlayDoh - generalized Cydra 5
  - Intel and HP's IA-64 - full predication
- *If-Conversion* is the process by which control flow is removed through the use of predication.
- *Reverse If-Conversion* is the process by which predication is removed through the introduction of control flow.



## Uses of Predication

- *Predicated Representation* - A program representation in which instructions can be guarded by a Boolean source operand
  - Efficient model for compiler optimization and scheduling
  - Control transformations can be performed as simple optimizations.
  - Removal of control dependences affords optimization and scheduling freedom.
- *Predicated Execution* - An architectural model which supports direct execution of the predicated representation
  - Allows removal of branch mispredictions through elimination of branches
  - Increases ILP by allowing concurrent execution of multiple program paths
  - Enables predicate-specific optimizations such as height reduction

## Predicate Defining Instructions

$$P_{d0\langle type_0 \rangle}, P_{d1\langle type_1 \rangle} = ( src_0 \text{ cond } src_1 ) \langle P_g \rangle$$

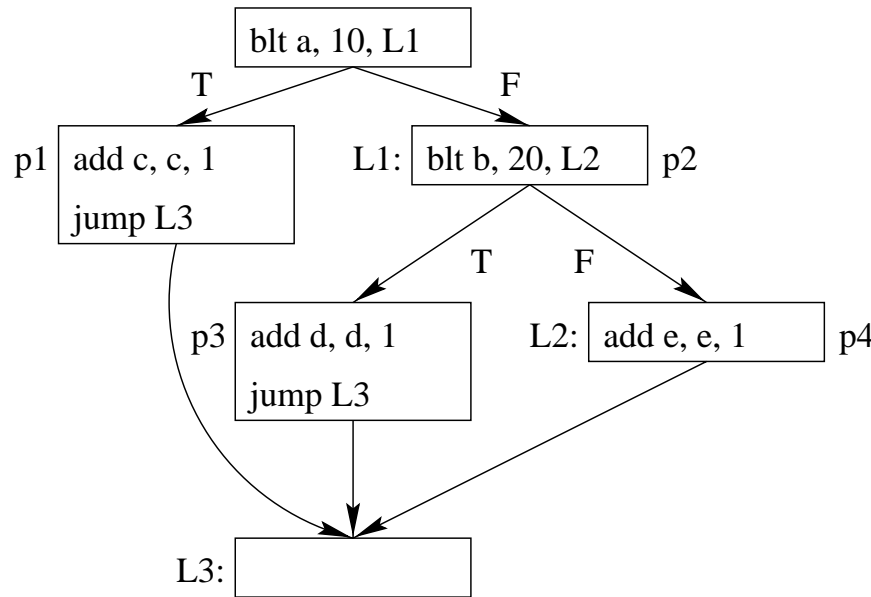
- *cond* comparison: =, <, ≤, etc.
- *type<sub>i</sub>* assignment type:
  - UT/UF - Unconditional
  - OT/OF - Wired-or
  - AT/AF - Wired-and
  - CT/CF - Conditional
  - ∨T/∨F - Disjunctive
  - ∧T/∧F - Conjunctive

# Unconditional Predicate Define

Generate a predicate for a block which executes on a single condition.

```

if ( a < 10 )
    c = c + 1;
else
    if ( b < 20 )
        d = d + 1;
    else
        e = e + 1;
    
```

$$\begin{aligned}
 p1_{UT}, p2_{UF} &= (a < 10) \\
 c = c + 1 &\langle p1 \rangle \\
 p3_{UT}, p4_{UF} &= (b < 20) \langle p2 \rangle \\
 d = d + 1 &\langle p3 \rangle \\
 e = e + 1 &\langle p4 \rangle
 \end{aligned}$$


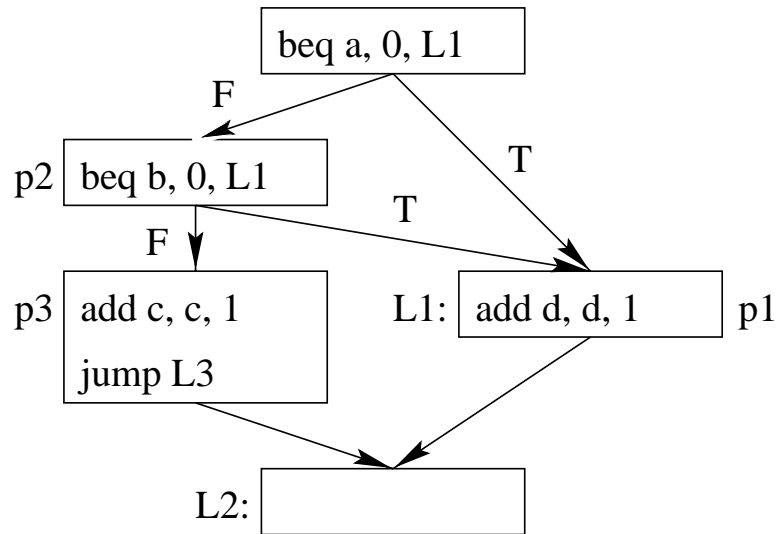
$P_g$	Comparison	$P_d$	
		UT	UF
0	0	0	0
0	1	0	0
1	0	0	1
1	1	1	0

# Wired-OR Predicate Define

Generate a predicate for a block which executes on multiple conditions.

```

if ( a && b )
    c = c + 1;
else
    d = d + 1;
    
```

$$\begin{aligned}
 & p1 = 0 \\
 & p1_{OT}, p2_{UF} = (a == 0) \\
 & p1_{OT}, p3_{UF} = (b == 0) \langle p2 \rangle \\
 & c = c + 1 \langle p3 \rangle \\
 & d = d + 1 \langle p1 \rangle
 \end{aligned}$$


$P_g$	Comparison	$P_d$	
		OT	OF
0	0	-	-
0	1	-	-
1	0	-	1
1	1	1	-



# Wired-AND Predicate Define

Generate a predicate for a block which executes on multiple conditions.

```

if ( a && b )
    c = c + 1;
else
    d = d + 1;
    
```

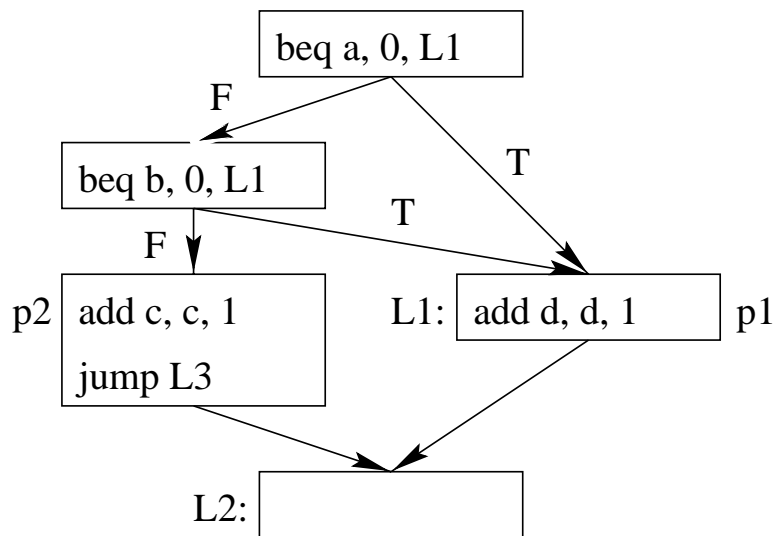
$$p1 = 0$$

$$p2 = 1$$

$$p1_{OT}, p2_{AF} = (a == 0)$$

$$p1_{OT}, p2_{AF} = (b == 0)$$

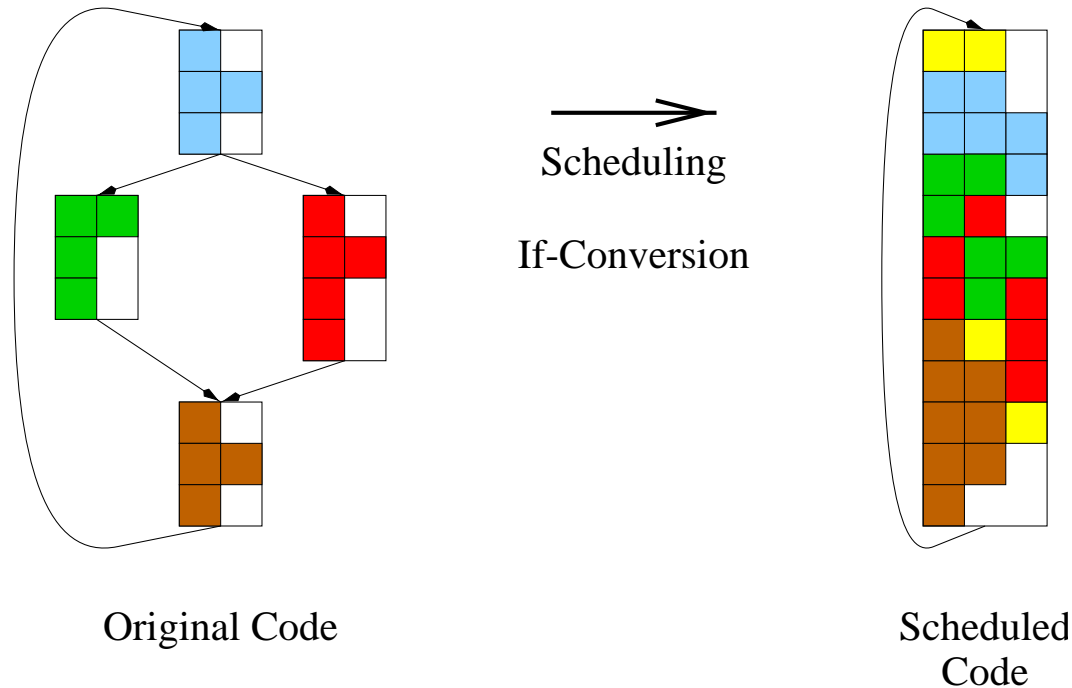
$$c = c + 1 \langle p2 \rangle$$

$$d = d + 1 \langle p1 \rangle$$


$P_g$	Comparison	$P_d$	
		AT	AF
0	0	-	-
0	1	-	-
1	0	0	-
1	1	-	0

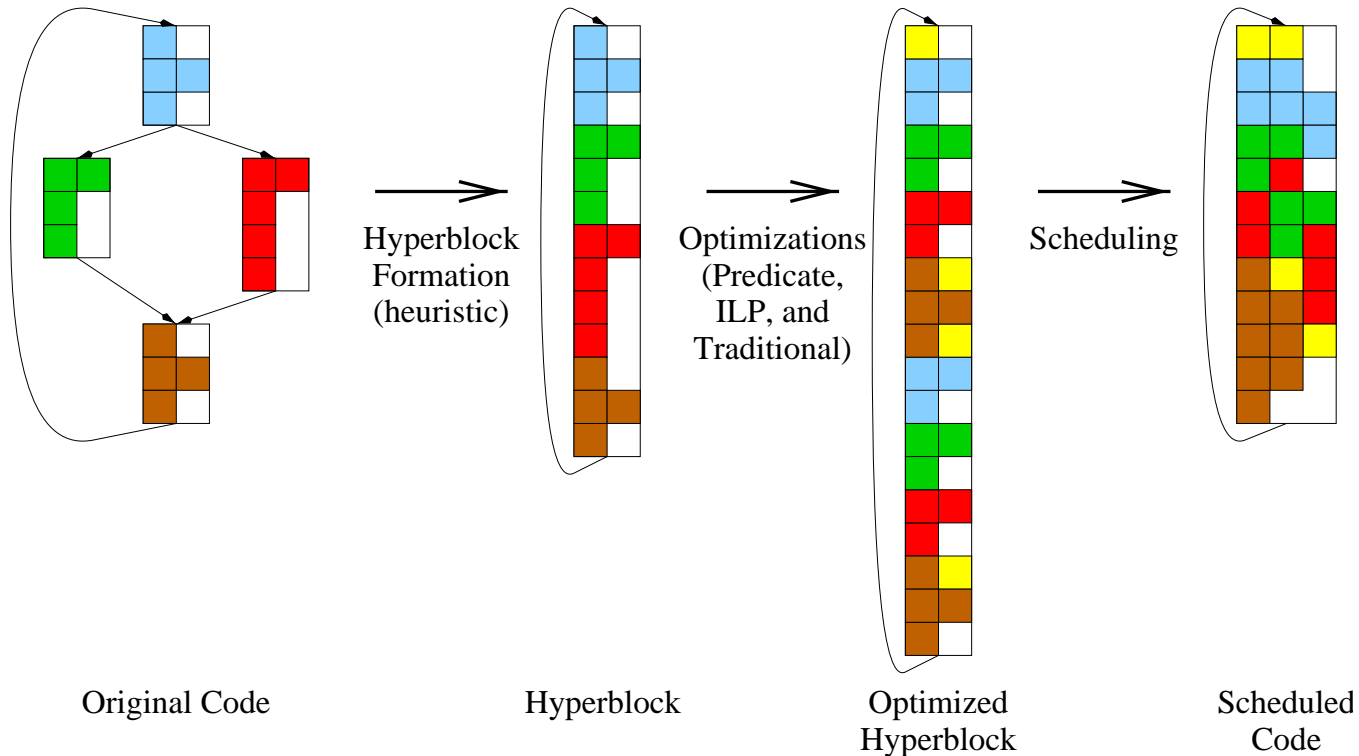
# The If-Conversion During Scheduling Framework

- Best time to balance control flow and predication
- Minimizes effect on existing compiler
- Naive - doesn't use predicated representation



# The Hyperblock Compilation Framework

- Current state-of-the-art in the IMPACT compiler.
- Framework is designed to generate efficient code for predicated execution.
- Early heuristic hyperblock formation estimates final code characteristics:

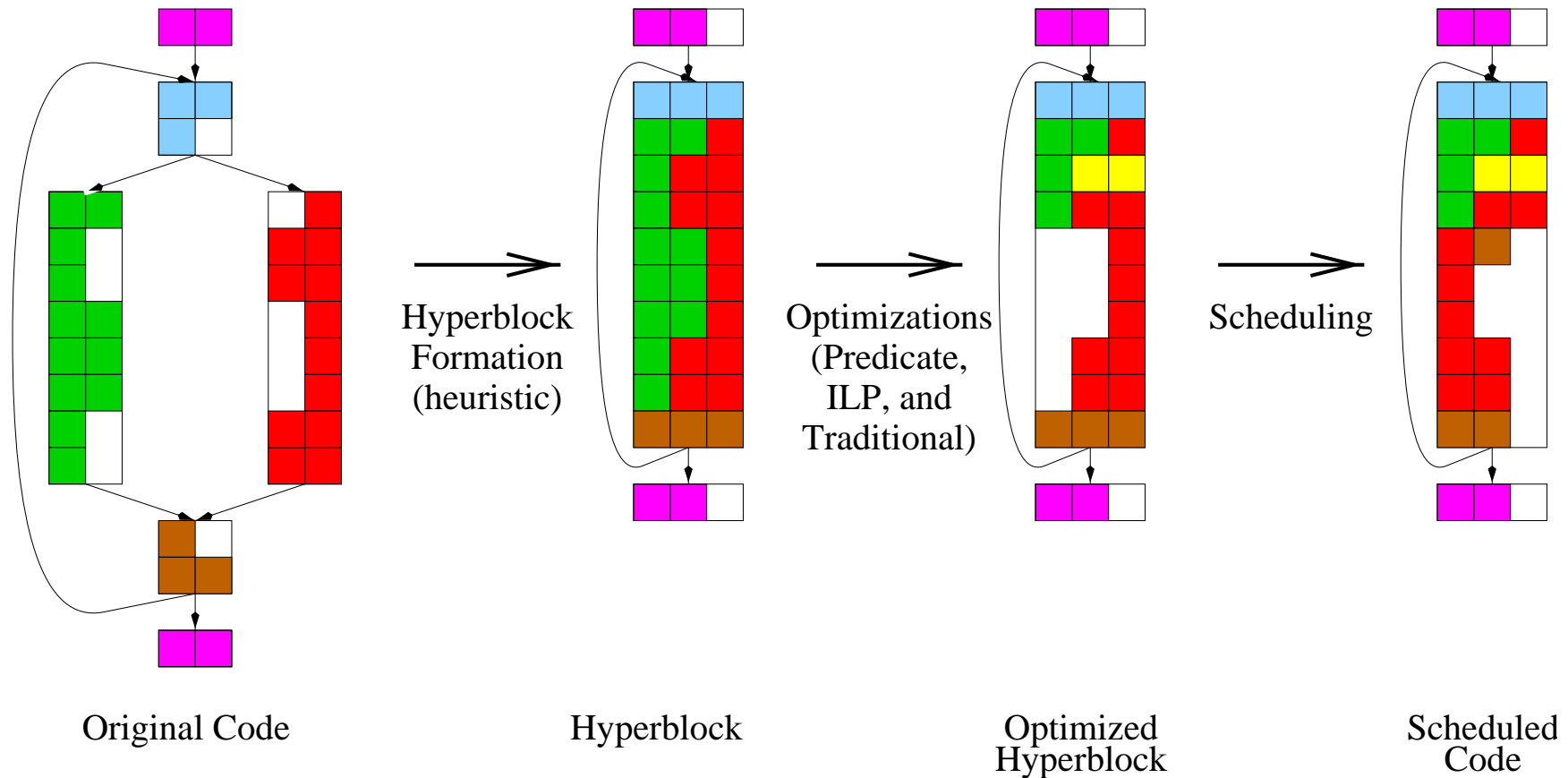


# Problems with Hyperblock Compilation Framework

- Phase Ordering
  - Strict phase-ordered creation of hyperblocks—early heuristic hyperblock formation, optimizations, then scheduling.
  - Interaction between resources and dependences is unpredictable.
  - Subsequent optimizations invalidate decisions made.
  - Estimates used in early heuristic hyperblock formation are not sufficiently fine-grained to include partial paths.
- Compilation Block Scope
  - Basic unit of compilation cannot contain loops.
  - Conservative hyperblock formation limits scheduling and optimization potential.
  - Conservative scope limits the types of transformations which can be applied.

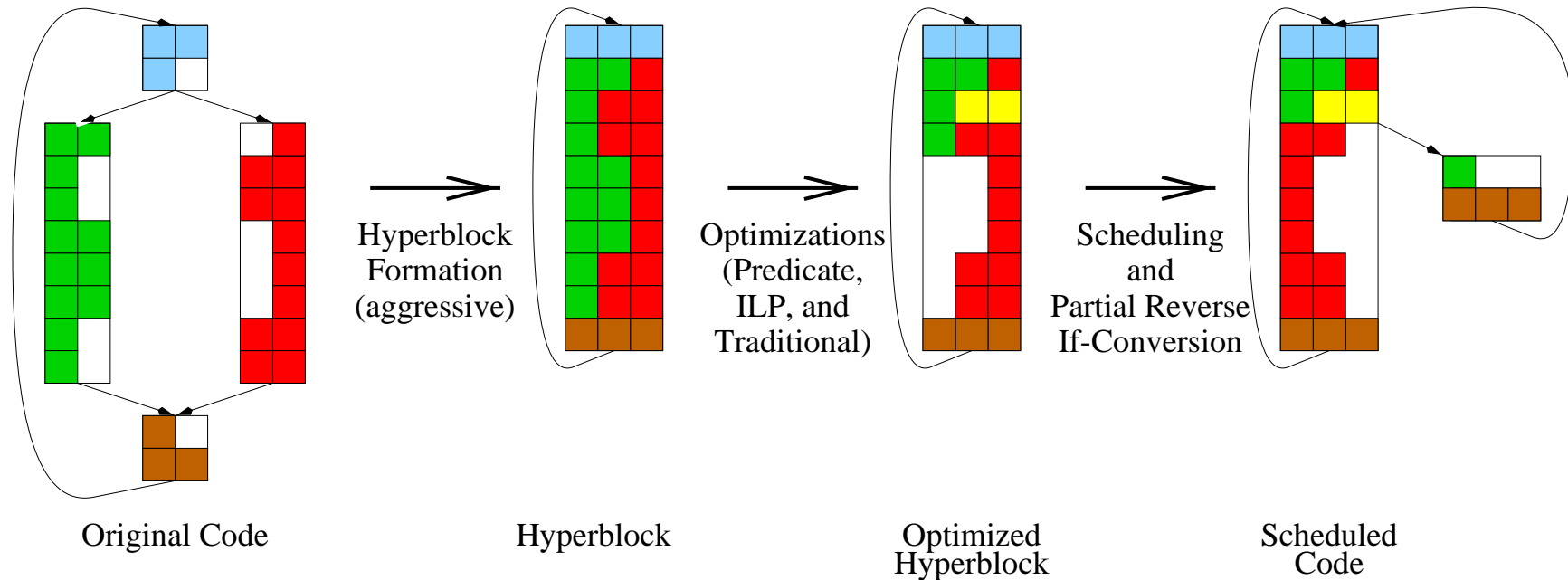
# Phase Ordering - The Optimization Problem

- Optimization changes a good hyperblock decision into a poor one:



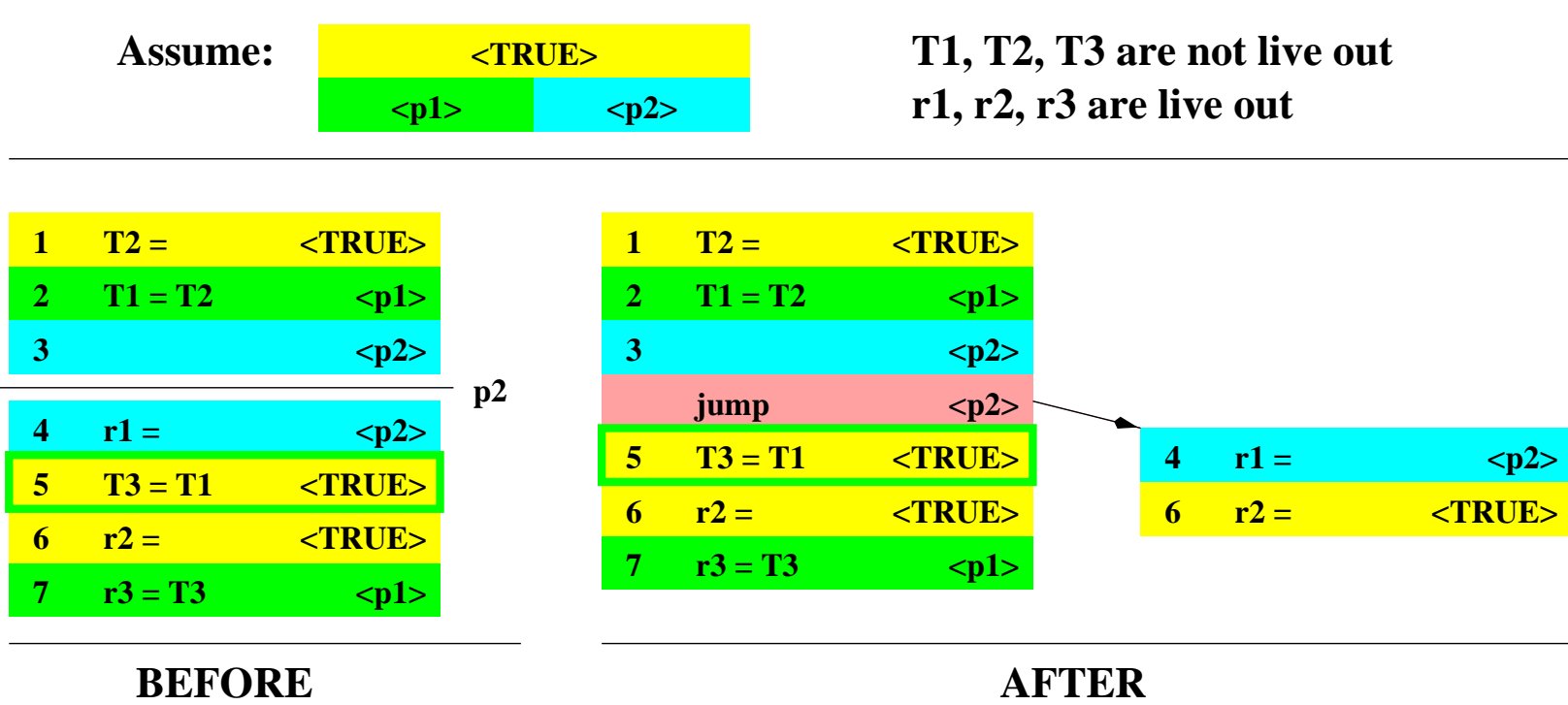
# Partial Reverse If-Conversion

- Overcomes the phase ordering problem
- Balances control flow and predication at schedule time
- Creates control flow after optimizations in the predicated representation

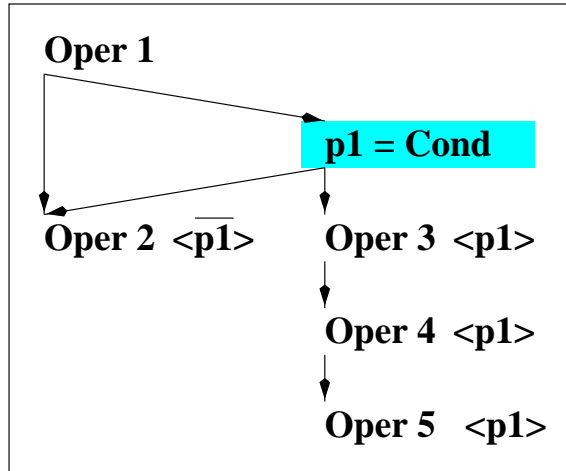


# Partial Reverse If-Conversion

- Partial Reverse If-Conversion Decision:
  - Two Part Decision: *Which* Predicate, *Where* In Schedule
  - Consider: Resources, Dependence height, Hazards, Execution frequency
- Partial Reverse If-Conversion Mechanics:



# Partial Reverse If-Conversion Algorithm



Without Partial Reverse If-Conversion

Oper 1
<b>p1 = Cond</b>
Oper 2 <math>\langle p1 \rangle</math>
Oper 3 <math>\langle p1 \rangle</math>
Oper 4 <math>\langle p1 \rangle</math>
Oper 5 <math>\langle p1 \rangle</math>

?

With Partial Reverse If-Conversion

Oper 1
--------

Oper 1
<b>p1 = Cond</b>

Oper 1
<b>p1 = Cond</b>
<b>Jump p1</b>

Oper 1
<b>p1 = Cond</b>
<b>Jump p1</b>
Oper 2 <math>\langle \bar{p1} \rangle</math>

Oper 3 <math>\langle p1 \rangle</math>
Oper 4 <math>\langle p1 \rangle</math>
Oper 5 <math>\langle p1 \rangle</math>

Ready:  
**p1 = Cond**

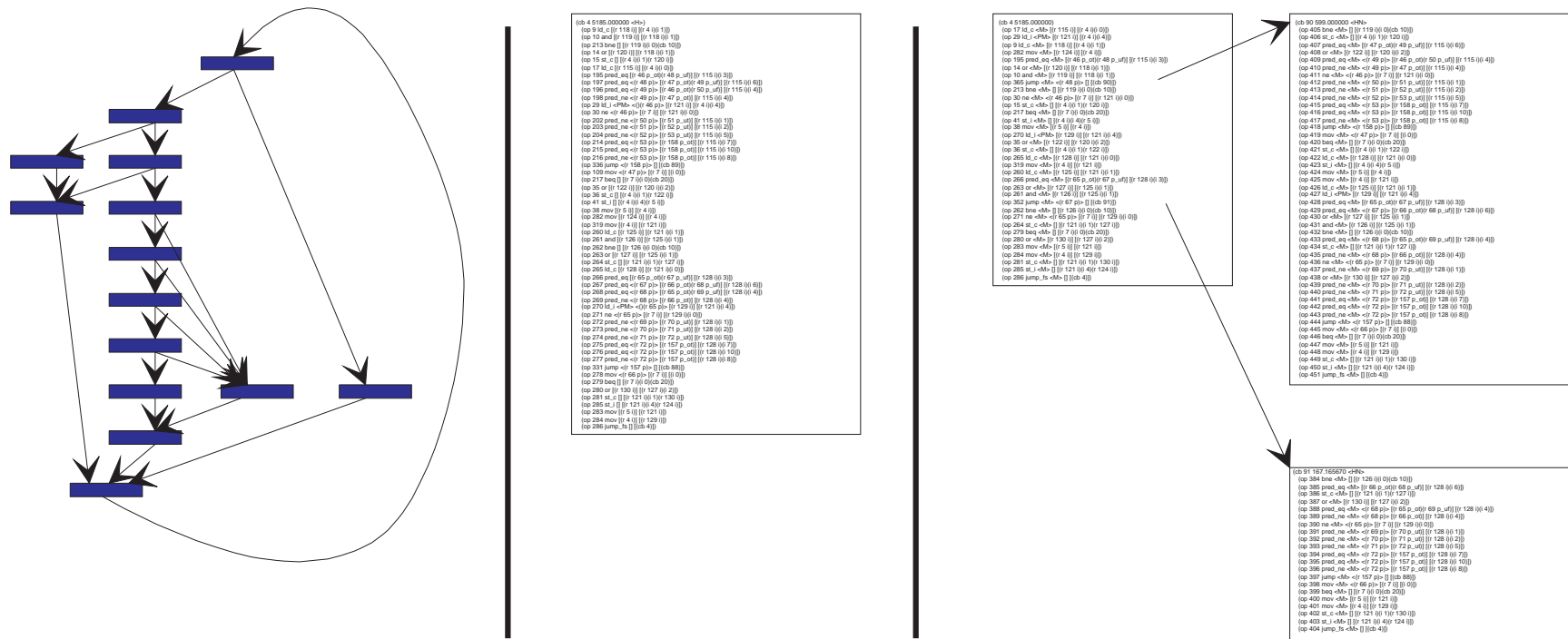
Ready:  
Oper 2 <math>\langle \bar{p1} \rangle</math>  
Oper 3 <math>\langle p1 \rangle</math>  
**Jump p1**

Ready:  
Oper 2 <math>\langle \bar{p1} \rangle</math>  
Oper 3 <math>\langle p1 \rangle</math>

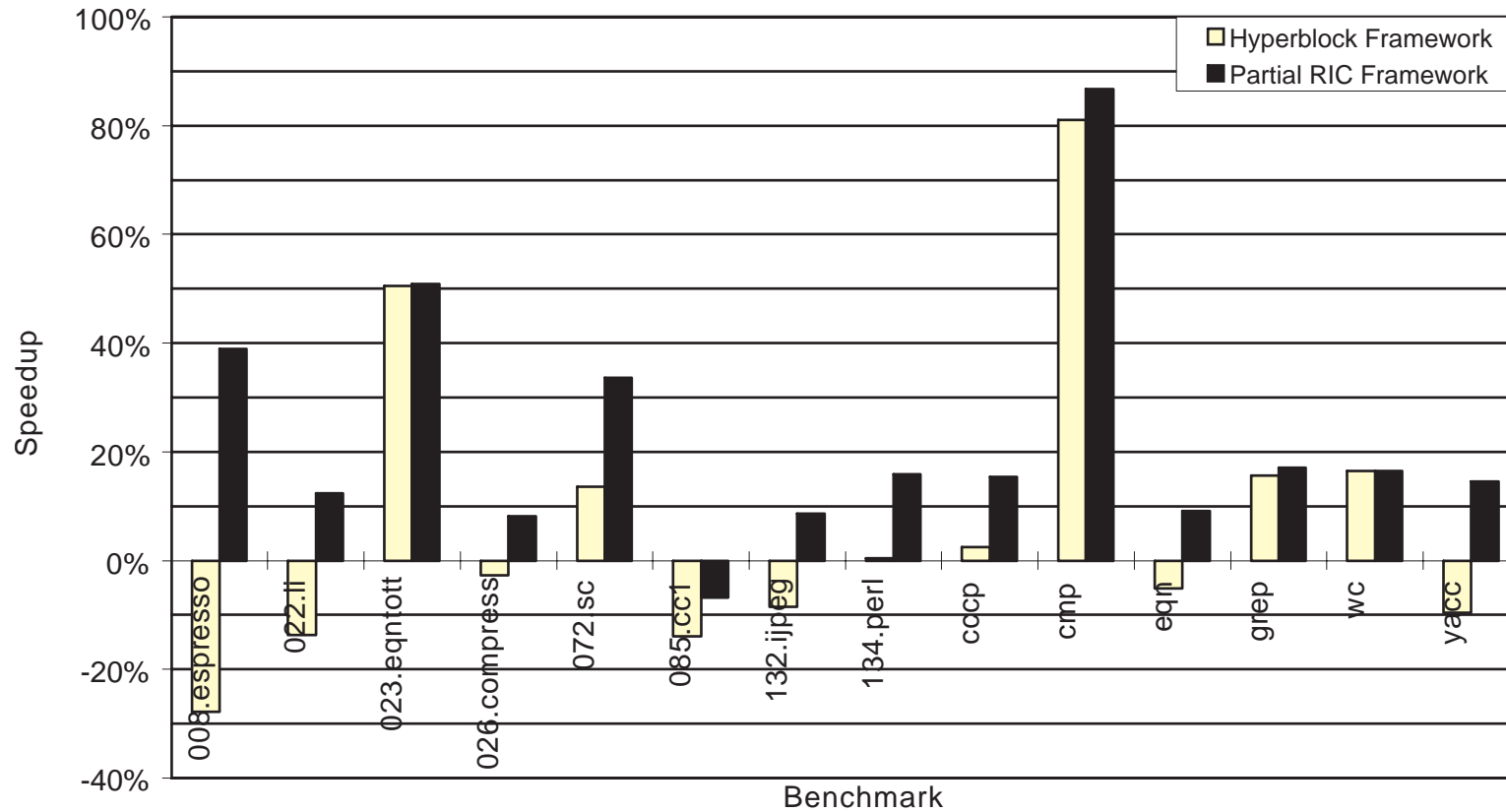


# Code Example

- In the function *\_mark* in the benchmark *022.li*:
  - 2 of 20 possible reverse if-conversions performed.
  - 58764 cycles → 38942 cycles → 34827 cycles



# Performance Improvement



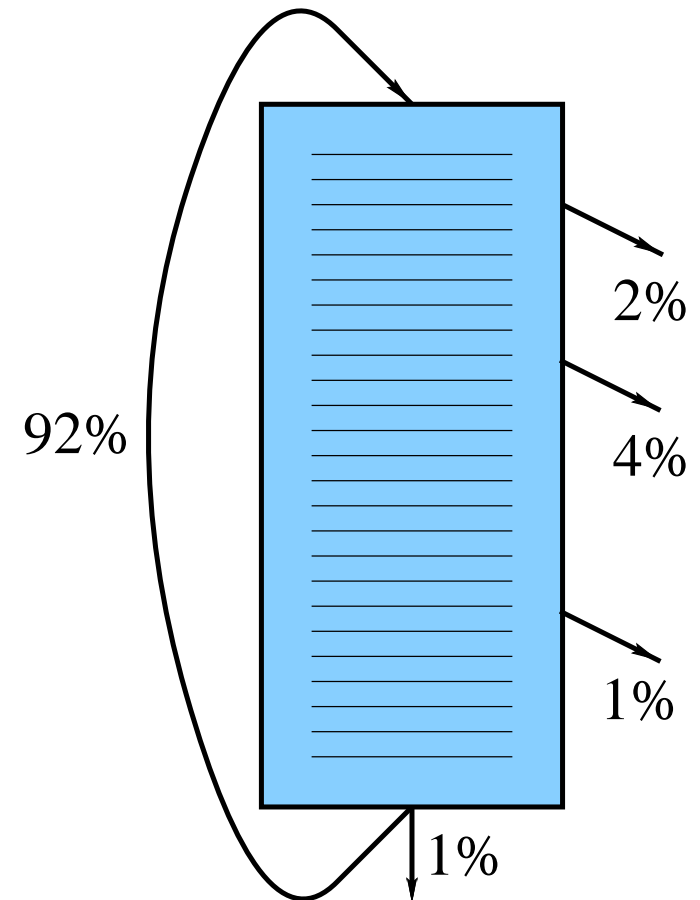
- No branch prediction penalty
- 4-issue: 1 branch, 2 integer, 2 memory, and 1 float

## Application Statistics

Benchmark	Reverse If-Conversions	Opportunities
008.espresso	204	1552
022.li	50	393
023.eqntott	43	443
026.compress	11	56
072.sc	33	724
085.cc1	479	3827
132.ijpeg	134	1021
134.perl	42	401
cccp	77	1046
cmp	4	49
eqn	33	326
grep	3	103
wc	0	88
yacc	247	1976

## Fully Resolved Predicates: Motivation

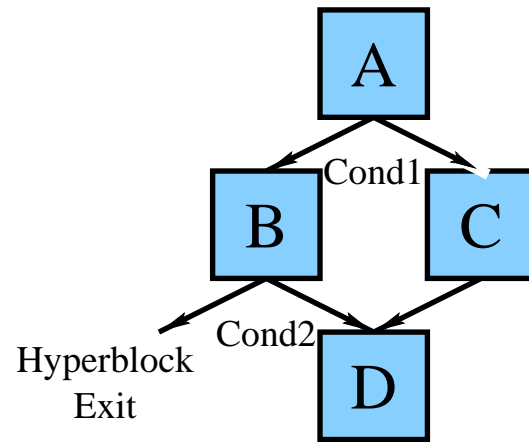
- Typical Hyperblocks and Superblocks have many infrequently taken exit branches.
- Infrequent exit branches
  - impede code motion
  - increase length of path to frequently taken branches
  - consume valuable branch resources
- Goal: Use predication to enhance performance in the presence of **easily predicted branches**.



## Fully Resolved Predicates: Concept

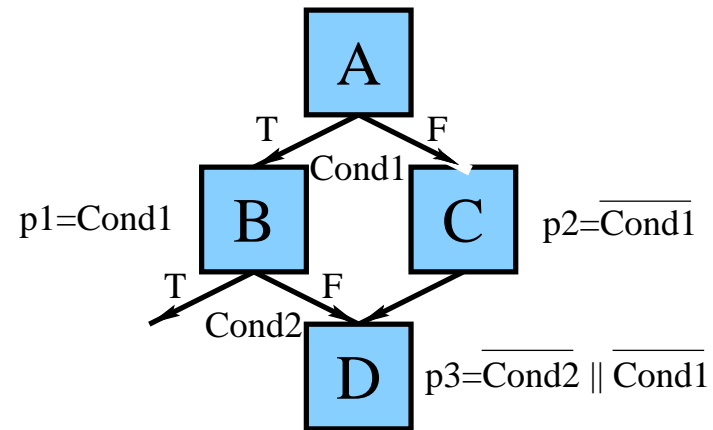
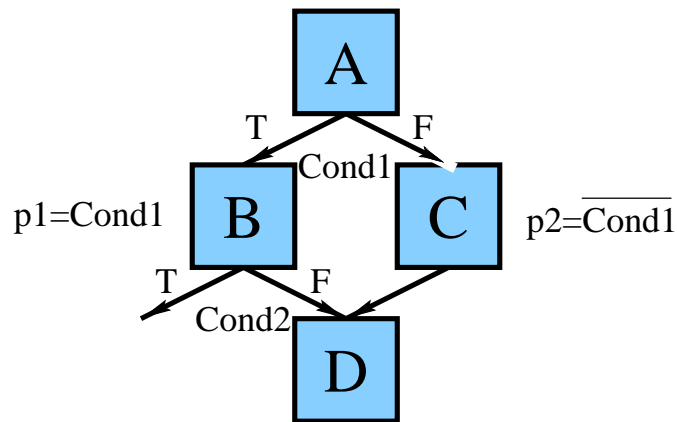
- Partially Resolved Predicates (PRP)
  - Instruction execution is guarded by predicates or branches.
  - Some control dependences remain in predicated code.
- Fully Resolved Predicates (FRP)
  - Instructions are guarded by predicates even if guarded by branches.
  - All control dependences within a region are eliminated.
  - Any instruction can be hoisted above a branch without speculation.

# Fully Resolved Predicates: Computation



Partially Resolved Predicates

Fully Resolved Predicates



# Fully Resolved Predicates: Optimization Opportunities

- Branch reordering
  - Branches can be placed in any order.
  - Move more frequently taken branches above less frequently taken branches.
- Instruction percolation without speculation
  - Percolated instructions can never have side effects because they are guarded by predicates.
  - Store instructions
    - \* Speculating stores has traditionally been problematic for most speculation schemes.
    - \* Inability to speculate stores limits available ILP.

## Fully Resolved Predicates: Case Study

- *grep* function “execute” inner loop
- Segment accounts for about 40% of total execution time.
- Source:

```
for ( ; ; )
{
    if (p2 >= ebp)
        /* Excluded from Hyperblock */
        if ((c = *p2++) == '\n')
            break;
    if (c)
        if (p1 < &linebuf[1024-1])
            *p1++ = c;
}
```



# Fully Resolved Predicates: Code Example

Original Code Segment:

CB 6:			Taken Frequency	
1	r35 = MEM[r34]	branch r34 >= r37, CB 95	14	
2	r34 = r34 + 1			
3		branch r35 == 10, CB 11	4035	
4		branch r35 == 0, CB 11	0	
5		branch r33 >= r57, CB 11	0	
6	MEM[r33] = r35	r33 = r33 + 1	jump CB 6	101148

FRP Predicated Code Segment:

CB 6:			Taken Frequency	
1	r35 = MEM[r34]	p0 <sub>ut</sub> , p1 <sub>uf</sub> = (r34 >= r37)		
2	r34 = r34 + 1 <p1>		jump CB 95 <p0>	14
3	p2 <sub>ut</sub> , p3 <sub>uf</sub> = (r35 == 10) <p1>			
4	p4 <sub>ut</sub> , p5 <sub>uf</sub> = (r35 == 0) <p3>		jump CB 11 <p2>	4035
5	p6 <sub>ut</sub> , p7 <sub>uf</sub> = (r33 >= r57) <p5>		jump CB 11 <p4>	0
6	MEM[r33] = r35 <p7>	r33 = r33 + 1 <p7>	jump CB 6 <p7>	101148
7			jump CB 11 <p6>	0

# Path Height Reduction: Concept

- Path Classes
  - dependence limited
  - resource limited
- Optimizations can be performed to exchange dependence height for resource usage
- Goal: balance resource height and dependence height to **reduce effective height of path**

Sequential code:


Saturated code:


- Height goes from 6 to 2
- Operation count went from 10 to 14
- Extra operations absorbed by processor width

# Path Height Reduction: Concept

Original:

$$T1 = A \circ B$$

$$T2 = T1 \circ C$$

$$E = T2 \circ D$$

Single back substitution:

$$T1 = A \circ B$$

$$E = T1 \circ C \circ D$$

Final:

$$E = A \circ B \circ C \circ D$$

Arithmetic Semantics—Tree of Computation:

$$T1 = A \circ B \quad T2 = C \circ D$$

$$E = T1 \circ T2$$

Parallel Semantics:

$$E \circ = A \circ B \quad E \circ = C \circ D$$

“ $\circ$ ” represents the universal associative operator.

# FRP/PHR: Code Example

FRP Predicated Code Segment:

CB 6:				Taken Frequency
1	r35 = MEM[r34]	p0 <sub>ut</sub> , p1 <sub>uf</sub> = (r34 >= r37)		
2	r34 = r34 + 1 <p1>		jump CB 95 <p0>	14
3	p2 <sub>ut</sub> , p3 <sub>uf</sub> = (r35 == 10) <p1>			
4	p4 <sub>ut</sub> , p5 <sub>uf</sub> = (r35 == 0) <p3>		jump CB 11 <p2>	4035
5	p6 <sub>ut</sub> , p7 <sub>uf</sub> = (r33 >= r57) <p5>		jump CB 11 <p4>	0
6	MEM[r33] = r35 <p7>	r33 = r33 + 1 <p7>	jump CB 6 <p7>	101148
7			jump CB 11 <p6>	0

FRP Predicated Code Segment with Height Reduction:

CB 6:				Taken Frequency
1	r35 = MEM[r34]	p0 <sub>ut</sub> , p1 <sub>uf</sub> = (r34 >= r37)	p7 <sub>af</sub> = (r34 >= r37)	
2	r34 = r34 + 1 <p1>	p7 <sub>af</sub> = (r33 >= r57)	jump CB 95 <p0>	14
3	p2 <sub>ut</sub> , p3 <sub>uf</sub> = (r35 == 10) <p1>	p7 <sub>af</sub> = (r35 == 10)	p7 <sub>af</sub> = (r35 == 0)	
4	MEM[r33] = r35 <p7>	r33 = r33 + 1 <p7>	jump CB 6 <p7>	101148
5	p4 <sub>ut</sub> , p5 <sub>uf</sub> = (r35 == 0) <p3>		jump CB 11 <p2>	4035
6	p6 <sub>ut</sub> = (r33 >= r57) <p5>		jump CB 11 <p4>	0
7			jump CB 11 <p6>	0

## FRP/PHR: *grep* Code Example Performance

Cycle	Original HB	FRP Only	FRP w/ Height Red.
1	14		
2		14	14
3	4035		
4	0	4035	101148
5	0	0	4035
6	101148	101148	0
7		0	0

Cycles	619007	623056	424795
Speedup	1.00	0.99	1.46

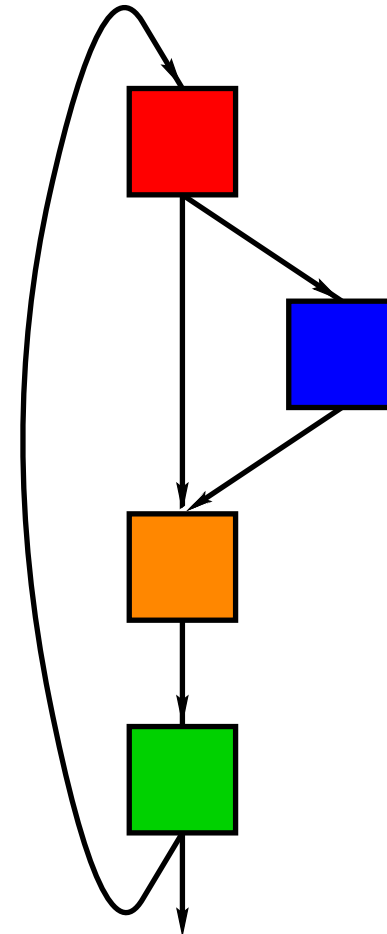
- FRP enabled a 46% speedup for a single iteration.
- Performance of this optimization is magnified by unrolling.

# Code Specialization: Case Study

- *compress* function “compress” inner loop
- Source:

```

probe:
{
  if ((i -= disp) < 0)
    i += hsize_reg;
  if (htabof(i) == fcode)
    /* Excluded from Hyperblock */
  if (htabof(i) > 0)
    goto probe;
}
    
```



# Code Specialization: Code Example

Original Code Segment	Specialized Code Segment
CB 38: 1 $r9 = r9 - r12$ 2 $(p1_{uf}) = (r9 < 0)$ 3 $r9 = r9 + r13$ (p1) 4 $r10 = r9 \ll 2$ 5 $r114 = MEM[r10]$ 6 7 $branch(r14 \ll r8) CB\ 38$	CB 38: 1 $r9 = r9 - r12$ 2 $(p1_{uf}, p2_{ut}) = (r9 < 0)$ 3 $r110 = r9 \ll 2$ (p2) $r9 = r9 + r13$ (p1) 4 $r114 = MEM[r110]$ (p2) $r10 = r9 \ll 2$ (p1) 5 $r14 = MEM[r10]$ (p1) 6 $branch(r114 \ll r8) CB\ 38$ (p2) 7 $branch(r14 \ll r8) CB\ 38$ (p1)

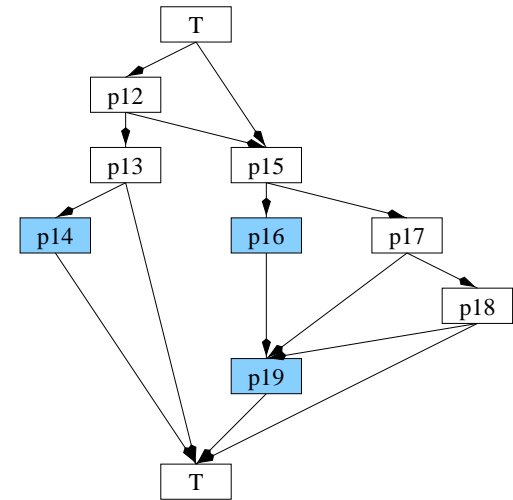
## Specialized Code Segment After Optimization

$r1312 = r13 - r12$		
CB 38:		
1	$r9 = r9 - r12$	$r1009 = r9 + r1312$
2	$r110 = r9 \ll 2$	$(p1_{uf}, p2_{ut}) = (r9 < 0)$
3	$r14 = MEM[r110]$ (p2)	$r9 = r1009$ (p1)
4		$r14 = MEM[r10]$ (p1)
5	$branch(r14 \ll r8) CB\ 38$	

# Advanced Control Flow Transformation

Original predicate definition schedule

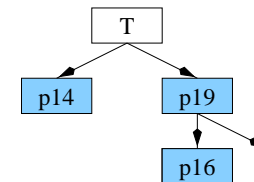
p15_of, p12_ut = (r4 > 32)	<T>		
p15_of, p13_ut = (r4 < 127)	<p12>		
p14_ut = (0 == r2)	<p13>	p16_ut, p17_uf = (r4 == 10)	<p15> p19_ot = (r4 == 10) <p15>
p19_ot, p18_uf = (r4 == 32)	<p17>		
p19_ot = (r4 == 9)	<p18>		



	Original predicate expressions	Expressed in terms of conditions	Minimized
	p12 c1	c1	
	p13 p12 & c2	c1 & c2	
	p14 p13 & c3	c1 & c2 & c3	c1 & c2 & c3
	p15 !c1   p12 & !c2	!c1   c1 & !c2	
	p16 p15 & c4	(!c1   c1 & !c2) & c4	c4
	p17 p15 & !c4	(!c1   c1 & !c2) & !c4	
	p18 p17 & !c5	((!c1   c1 & !c2) & !c4) & !c5	
	p19 p15 & c4   p17 & c5   p18 & c6	(!c1   c1 & !c2) & c4   ((!c1   c1 & !c2) & !c4) & c5   (((!c1   c1 & !c2) & !c4) & !c5) & c6	c4   c5   c6

Predicate definition schedule after range analysis and and-type parallelization

p14_at = (r4 > 32)	<T>	p14_at = (r4 < 127)	<T>	p14_at = (r2 == 0)	<T>	...	
...		p19_ot, p16_ut = (r4 == 10)	<T>	p19_ot = (r4 == 32)	<T>	p19_ot = (r4 == 9)	<T>



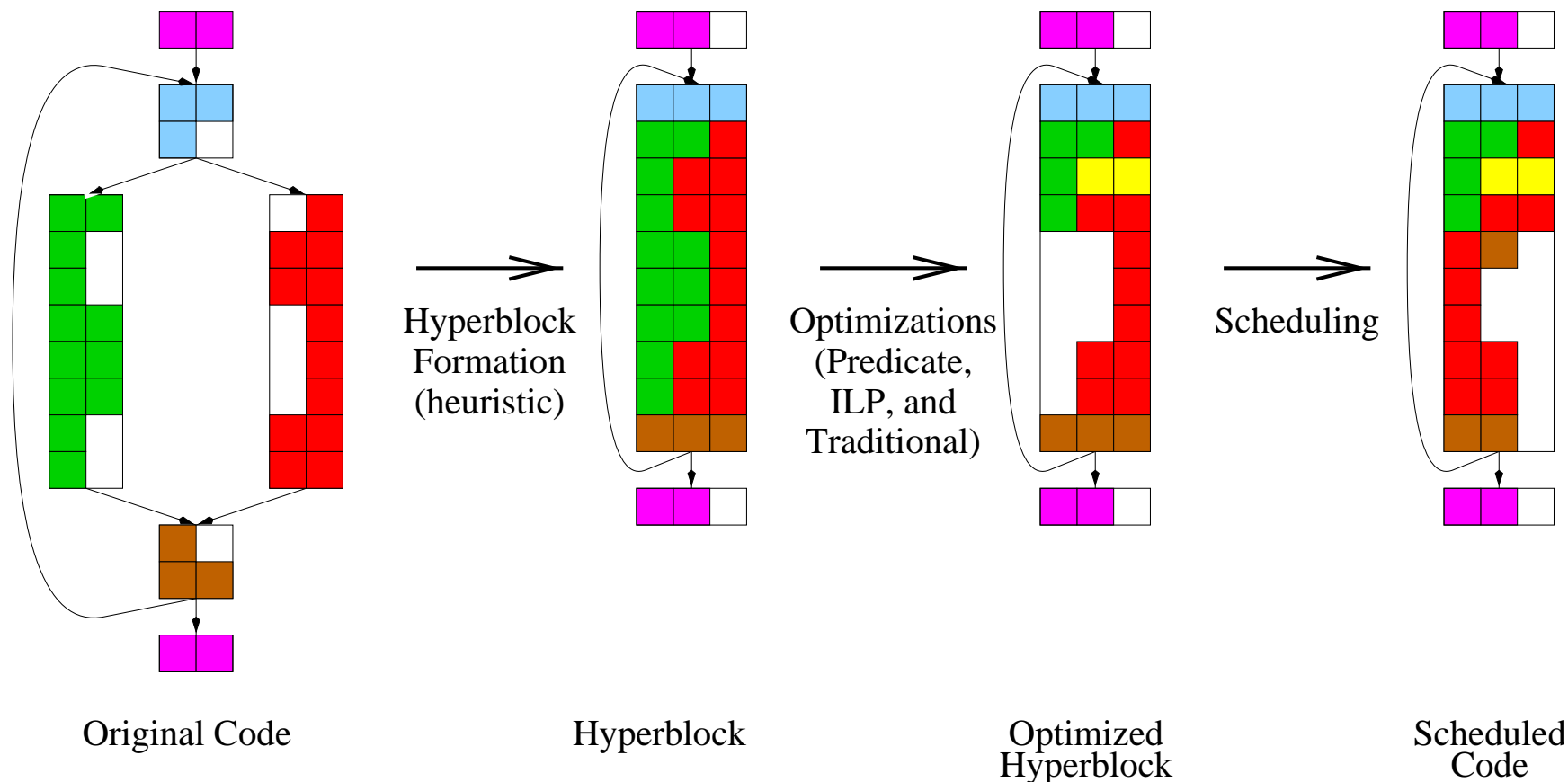


## Advanced Control Flow Transformation

- The predicated representation enables extraction and manipulation of program control logic.
- Optimization of predicate defines can be formulated as a specialized logic synthesis problem.
  - Predicate definitions are analogous to gates. They consume resources.
  - Predicate computation height is analogous to total gate delay.
  - Inputs may be available at different times.
  - Resource availability changes with the schedule.
- Algorithm overview:
  - Analyze conditions for interrelation.
  - Extract program control logic from extant predicate defines.
  - Minimize logical expressions using Boolean optimization techniques.
  - Factor control expressions based on condition availability and schedule freedom.
  - Re-express control as a new, optimized predicate define network.

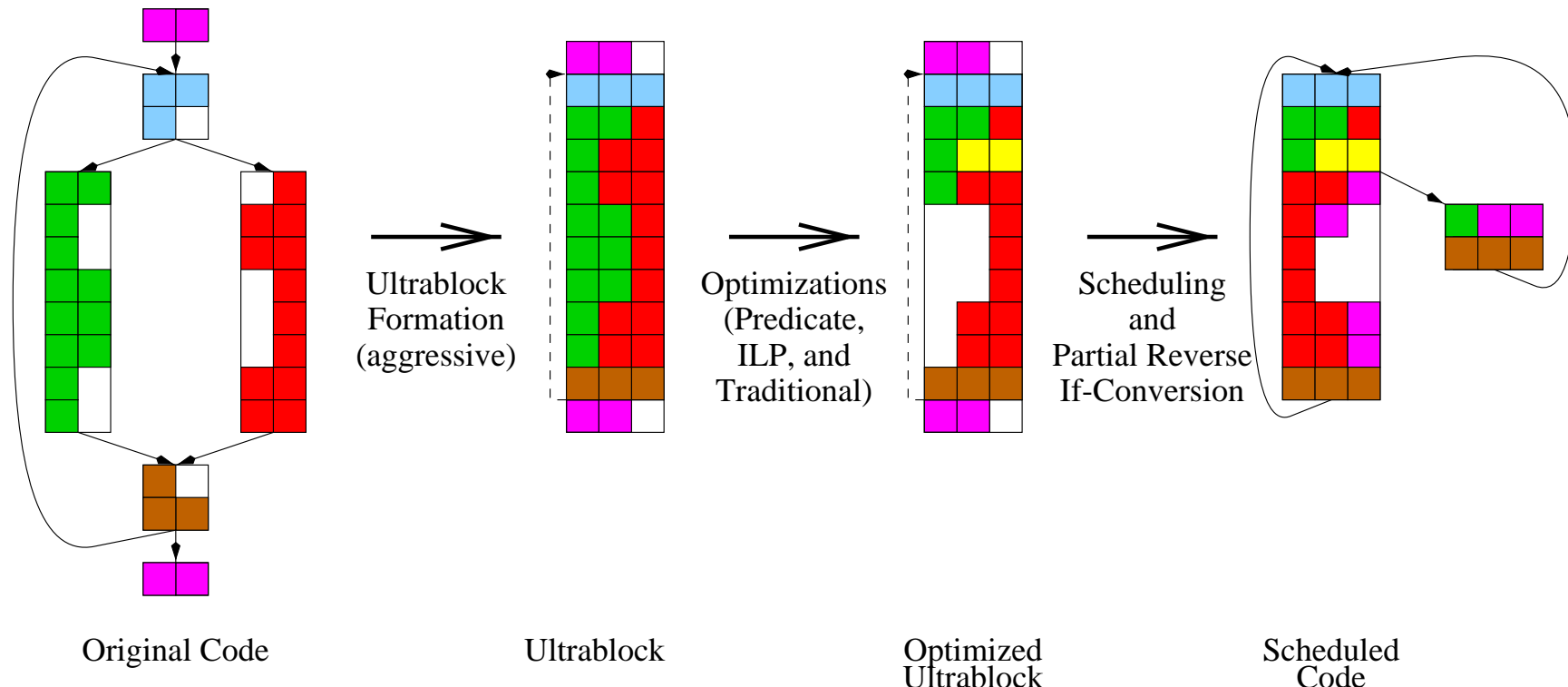
# Compilation Block Scope - The Loop Boundary Problem

- Acyclic nature of hyperblocks precludes pre-loop and post-loop block subsumption.



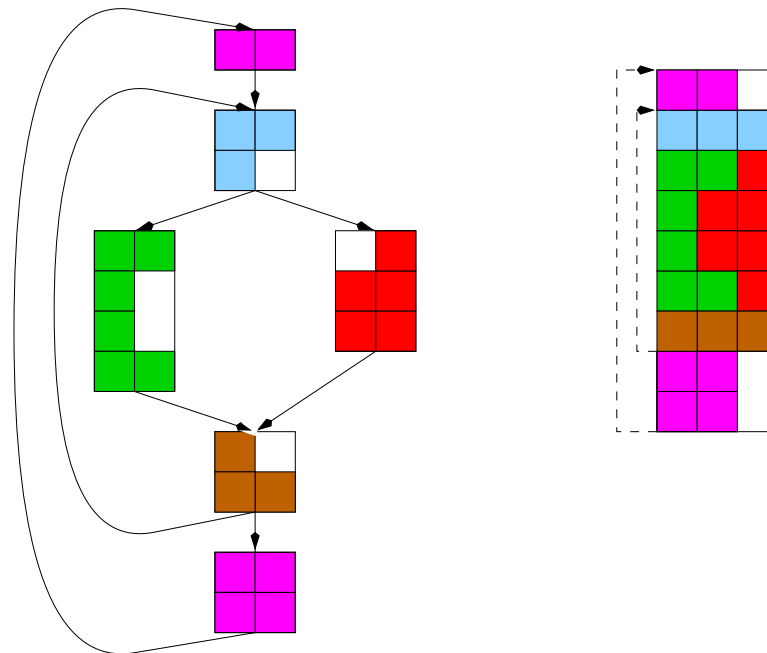
# The Ultrablock Compilation Framework

- Best use of predicated representation: Early aggressive formation which can support generalized regions
- Best use of predicated execution: Partial Reverse If-Conversion for scheduler adjustment of predication and reinstantiation of control flow



# Intermediate Representation

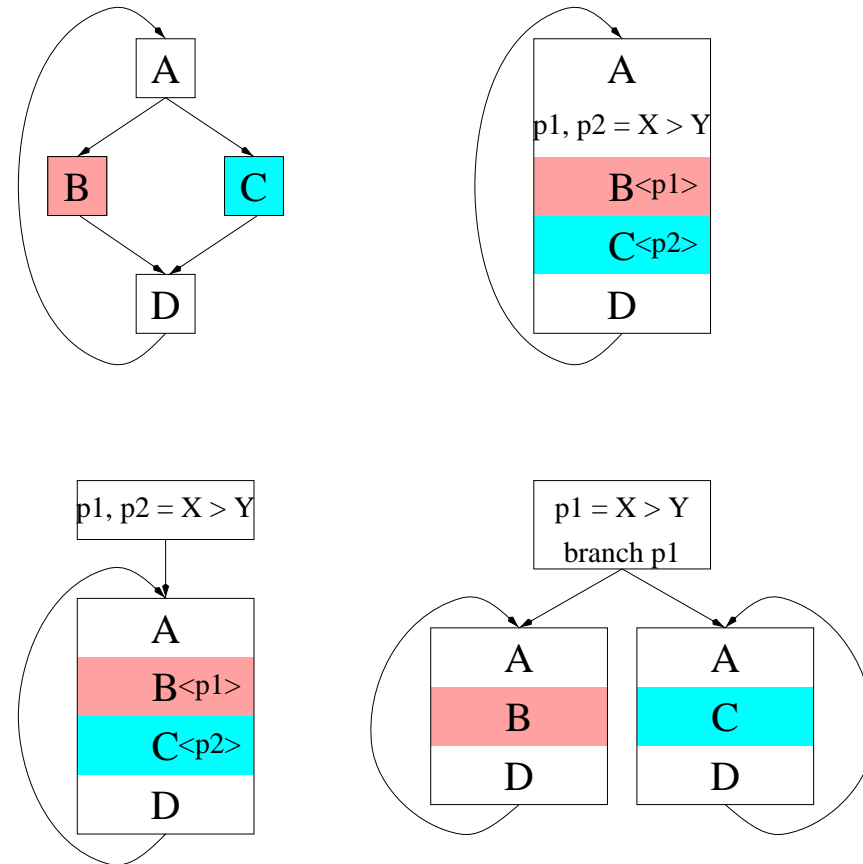
- IR needs to be extended to represent *ultrablocks* which can represent internal cycles to support compilation of general regions.
- Special purpose control flow and loop transformations can be replaced by data flow optimizations.
- A few techniques possible with current data flow optimizations are: loop versioning, loop fusion, if-then-else fusion, if-then-else interchange.



# Ultrablock Example: Loop Versioning

Few compilers do loop versioning, probably because it is a complicated and/or expensive control flow transformation.

- 3,608,541 dynamic loop iterations in 085.cc1
- 1,309,548 (36%) of these iterations have *loop invariant, program variant* branches and predicates.
- 374,279 (10%) of these iterations have *loop invariant, program variant* predicates.



# Predicate Analysis

- Predicate Analysis analyzes predicate definitions to understand how predicates relate to one another.
- This information is essential for the compilation process.
  - Optimization
  - Register Allocation
  - Scheduling
- Predicate analysis applied to optimization—constant propagation example:

$p1_{ut} = cond1$	$p2_{ut}, p1_{ot} = cond1$	$p1_{ut}, p2_{at} = cond1$
$p2_{ut} = cond2 < p1 >$	$p1_{ot} = cond2$	$p2_{at} = cond2$
If $p1$ is a superset of $p2$ :		
$r1 = 10 < p1 > \implies r2 = 12 < p2 >$ $r2 = r1 + 2 < p2 >$		

## Predicate Analysis—Related Work

- Predicate Analysis has traditionally been done hierarchically.
- Predicate Hierarchy Graph (PHG), the original system in IMPACT, is purely hierarchical.
- Unfortunately, predicates are not always related in a hierarchical fashion and these systems cannot accurately represent all relationships.

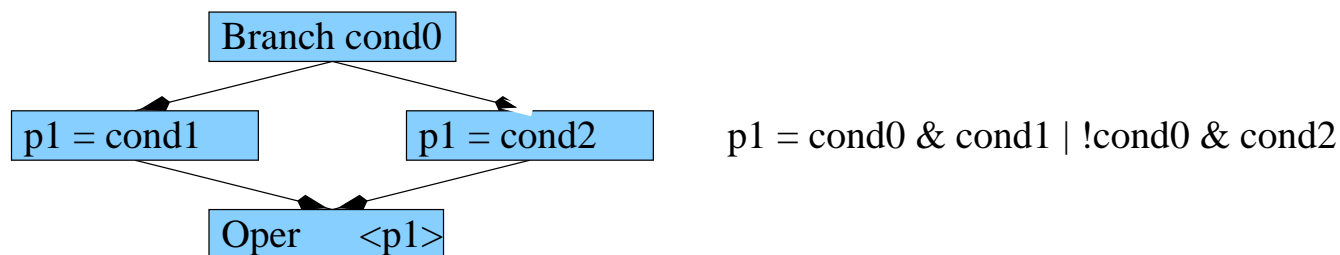
$$\begin{array}{l}
 p2_{ut}, p1_{ot} = cond1 \\
 p1_{ot} = cond2 \\
 p3_{ut} = cond3 < p2 >
 \end{array}$$

$p1$  is not an ancestor of  $p3$ , but  $p1$  is a superset of  $p3$ .

- Predicate Query System (PQS) - used in the *Elcor* compiler at HP Labs makes approximations in other ways.

## The Predicate Analysis System (PAS)

- Predicate definitions are essentially Boolean expressions — leverage CAD work in Boolean representations to represent all predicate relations.
- The PAS is built upon Binary Decision Diagrams (BDDs) — specifically, PAS was built upon *Cudd*. [Somenzi]
- In addition to being unable to represent all relations, the PHG and PQS are:
  - limited locally to a single hyperblock.
  - not able to understand branch guards.



- PAS can represent instruction guarding by branches and predicates.
- Each instruction in the program has a complete expression of its execution, with the exception of loops.



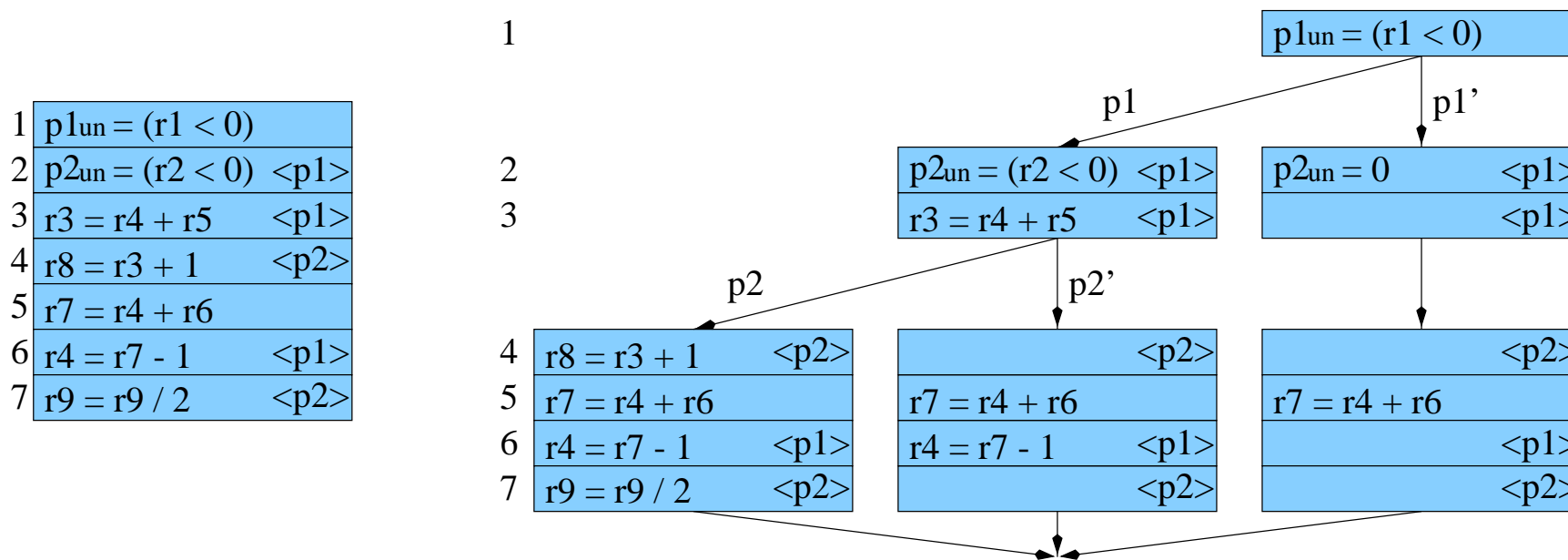
## Dataflow Analysis

- Dataflow can be performed without regard to predicates; results are conservative.
- Conservative results make optimizations, scheduling, and register allocation less effective.
- Conservative dataflow
  - Only instructions on TRUE can KILL.
  - r3 is not killed by instruction 3 because it is predicated.
  - The live range of r3 = {1, 2, 3, 4}.
- Predicate-aware dataflow
  - Instructions on a predicate KILL on that predicate.
  - The live range of r3 = {3, 4}.

1	$p1_{un} = (r1 < 0)$
2	$p2_{un} = (r2 < 0)$ <p1>
3	$r3 = r4 + r5$ <p1>
4	$r8 = r3 + 1$ <p2>
5	$r7 = r4 + r6$
6	$r4 = r7 - 1$ <p1>
7	$r9 = r9 / 2$ <p2>

# Dataflow Analysis—Predicate Flow Graph

- Developed the Predicate Flow Graph (PFG) which can perform predicate-sensitive dataflow analysis.
- Idea was to change the underlying graph so that traditional dataflow analysis techniques would generate correct results.
- Results have shown that accurate dataflow analysis has been achieved.



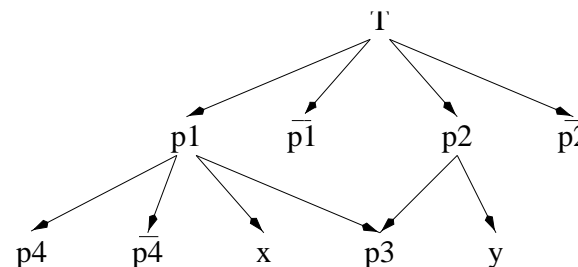
## Dataflow Analysis Path Explosion Problem

- Predication eliminates the need for many paths to exist in control flow.
- Using the PFG based approach these paths become materialized.
- As a general rule, the path width of the PFG is greater than  $2^n$ , where n is the number of independent predicates with overlapping live ranges.
- Assuming p1, p2, and p3 are independent we have  $2^3 = 8$  paths.

1	$p1_{un} = (r1 < 0)$	
2	$p2_{un} = (r2 < 0)$	
3	$p3_{un} = (r3 < 0)$	
4	$r5 = X$	<p1>
5	$r6 = Y$	<p2>
6	$Z = r5$	<p3>

# Dataflow Analysis: Disjunctive Compositions

- The key to eliminating the exponential nature of dataflow analysis is a partition graph of disjunctive expressions.
- By operating on a partition graph, interactions between independent predicates can be expressed without enumerating all paths.
- Predicates are composed of nodes, any two of which exist in exactly one of three relationships: *implication*, *independence*, or *exclusivity*.
- Using only such nodes guarantees that complex relationships between predicates can be represented exactly, yielding accurate dataflow results.



SSA pred. def.	Resulting disjunctive expressions
$p_{i,j} = \text{ut } C \langle p_g \rangle$	$p_{i,j} = p_g C$
$p_{i,j} = \text{uf } C \langle p_g \rangle$	$p_{i,j} = p_g C'$
$p_{i,j} = [p_{i,j-1}] \text{ot } C \langle p_g \rangle$	$p_{i,j} = p_g' p_{i,j-1} \vee p_g p_{i,j-1} C' \vee p_g C$
$p_{i,j} = [p_{i,j-1}] \text{of } C \langle p_g \rangle$	$p_{i,j} = p_g' p_{i,j-1} \vee p_g p_{i,j-1} C' \vee p_g C$
$p_{i,j} = [p_{i,j-1}] \text{ct } C \langle p_g \rangle$	$p_{i,j} = p_g' p_{i,j-1} \vee p_g C$
$p_{i,j} = [p_{i,j-1}] \text{cf } C \langle p_g \rangle$	$p_{i,j} = p_g' p_{i,j-1} \vee p_g C'$
$p_{i,j} = [p_{i,j-1}] \text{at } C \langle p_g \rangle$	$p_{i,j} = p_g' p_{i,j-1} \vee p_g p_{i,j-1} C$
$p_{i,j} = [p_{i,j-1}] \text{af } C \langle p_g \rangle$	$p_{i,j} = p_g' p_{i,j-1} \vee p_g p_{i,j-1} C'$

# A Global Predication Compilation Framework

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